

Instability of $\hat{a}$ CLL under OFE, even in the presence of pseudo-counts

Constants

```
beta = (Pi^2 - 18) / 24;  
alpha = (Pi^2 + 6) / 24;  
lambda = (Pi^2) / 6;
```

Case I dataset with 500 elements

■ Dataset values

```
Nijck = 400;  
  
Nijc = 410;  
  
(*Nij(1-c)*)  
Nijcc = 20;  
  
(*Nij(1-c)*)  
Nijcck = 0;
```

■ PseudoCounts 0.5

```
PC = 0.5;  
NijckPC = Nijck + PC;  
NijcPC = Nijc + 2 * PC;  
NijccPC = Nijcc + 2 * PC;  
NijcckPC = Nijcck + PC;
```

■ $\hat{a}$ CLL left summand

```
N[alpha NijckPC Log[2, NijckPC / NijcPC]]  
  
-9.88751
```

■ $\hat{a}$ CLL right summand (bad behaviour)

```
N[beta NijckPC Log[2, NijcckPC / NijccPC]]  
  
731.608
```

■ fCLL left summand

```
N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]  
  
-4.82189
```

■ fCLL right summand

```
N[-beta * lambda * NijckPC  
  (Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)])]  
  
15.6432
```

■

PseudoCounts 5

```
PC = 5;
NijckPC = Nijck + PC;
NijcPC = Nijc + 2 * PC;
NijccPC = Nijcc + 2 * PC;
NijcckPC = Nijcck + PC;
```

■ âCLL left summand

```
N[alpha NijckPC Log[2, NijckPC / NijcPC]]
- 14.0508
```

■ âCLL right summand (bad behaviour)

```
N[beta NijckPC Log[2, NijcckPC / NijccPC]]
354.658
```

■ fCLL left summand

```
N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]
- 6.8522
```

■ fCLL right summand

```
N[-beta * lambda * NijckPC
  (Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)])]
18.4687
```

■ PseudoCounts 10

```
PC = 10;
NijckPC = Nijck + PC;
NijcPC = Nijc + 2 * PC;
NijccPC = Nijcc + 2 * PC;
NijcckPC = Nijcck + PC;
```

■ âCLL left summand

```
N[alpha NijckPC Log[2, NijckPC / NijcPC]]
- 18.6284
```

■ âCLL right summand (bad behaviour)

```
N[beta NijckPC Log[2, NijcckPC / NijccPC]]
277.789
```

■ fCLL left summand

```
N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]
- 9.08461
```

■

■

fCLL right summand

```

N[-beta * lambda * NijckPC
  ( Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)] ) ]
21.3755

```

Case II dataset with 1000 elements
■ Dataset values that make $\hat{a}CLL$ diverge

```

Nijck = 800;

Nijc = 810;

(*Nij(1-c)*)
Nijcc = 30;

(*Nij(1-c)*)
Nijcck = 0;

```

■ PseudoCounts 0.5

```

PC = 0.5;
NijckPC = Nijck + PC;
NijcPC = Nijc + 2 * PC;
NijccPC = Nijcc + 2 * PC;
NijcckPC = Nijcck + PC;

```

■ $\hat{a}CLL$ left summand

```

N[alpha NijckPC Log[2, NijckPC / NijcPC]]
-9.95144

```

■ $\hat{a}CLL$ right summand (bad behaviour)

```

N[beta NijckPC Log[2, NijcckPC / NijccPC]]
1614.67

```

■ fCLL left summand

```

N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]
-4.85307

```

■ fCLL right summand

```

N[-beta * lambda * NijckPC
  ( Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)] ) ]
23.7391

```

■

■ PseudoCounts 5

```
PC = 5;
NijckPC = Nijck + PC;
NijcPC = Nijc + 2 * PC;
NijccPC = Nijcc + 2 * PC;
NijcckPC = Nijcck + PC;
```

■ âCLL left summand

```
N[alpha NijckPC Log[2, NijckPC / NijcPC]]
- 14.1777
```

■ âCLL right summand (bad behaviour)

```
N[beta NijckPC Log[2, NijcckPC / NijccPC]]
818.121
```

■ fCLL left summand

```
N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]
- 6.9141
```

■ fCLL right summand

```
N[-beta * lambda * NijckPC
  (Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)])]
26.8162
```

■ PseudoCounts 10

```
PC = 10;
NijckPC = Nijck + PC;
NijcPC = Nijc + 2 * PC;
NijccPC = Nijcc + 2 * PC;
NijcckPC = Nijcck + PC;
```

■ âCLL left summand

```
N[alpha NijckPC Log[2, NijckPC / NijcPC]]
- 18.8474
```

■ âCLL right summand (bad behaviour)

```
N[beta NijckPC Log[2, NijcckPC / NijccPC]]
637.139
```

■ fCLL left summand

```
N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]
- 9.19142
```

■

fCLL right summand

```

N[-beta * lambda * NijckPC
  (Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)])]
30.102

```

Case III for Large dataset with 10000 elements the problems are more acute
■ Dataset values that make $\hat{a}CLL$ diverge

```

Nijck = 9000;
Nijc = 9150;
(*Nij(1-c)*)
Nijcc = 70;
(*Nij(1-c)*)
Nijcck = 0;

```

■ PseudoCounts 0.5

```

PC = 0.5;
NijckPC = Nijck + PC;
NijcPC = Nijc + 2 * PC;
NijccPC = Nijcc + 2 * PC;
NijcckPC = Nijcck + PC;

```

■ $\hat{a}CLL$ left summand

```

N[alpha NijckPC Log[2, NijckPC / NijcPC]]
- 48.0402

```

■ $\hat{a}CLL$ right summand (bad behaviour)

```

N[beta NijckPC Log[2, NijcckPC / NijccPC]]
21800.1

```

■ fCLL left summand

```

N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]
- 23.428

```

■ fCLL right summand

```

N[-beta * lambda * NijckPC
  (Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)])]
56.1378

```

■

■ PseudoCounts 5

```
PC = 5;
NijckPC = Nijck + PC;
NijcPC = Nijc + 2 * PC;
NijccPC = Nijcc + 2 * PC;
NijcckPC = Nijcck + PC;
```

■ âCLL left summand

```
N[alpha NijckPC Log[2, NijckPC / NijcPC]]
- 146.605
```

■ âCLL right summand (bad behaviour)

```
N[beta NijckPC Log[2, NijcckPC / NijccPC]]
12 202.4
```

■ fCLL left summand

```
N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]
- 71.4958
```

■ fCLL right summand

```
N[-beta * lambda * NijckPC
  (Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)])]
58.9338
```

■ PseudoCounts 10

```
PC = 10;
NijckPC = Nijck + PC;
NijcPC = Nijc + 2 * PC;
NijccPC = Nijcc + 2 * PC;
NijcckPC = Nijcck + PC;
```

■ âCLL left summand

```
N[alpha NijckPC Log[2, NijckPC / NijcPC]]
- 151.294
```

■ âCLL right summand (bad behaviour)

```
N[beta NijckPC Log[2, NijcckPC / NijccPC]]
9675.52
```

■ fCLL left summand

```
N[(alpha + beta) NijckPC Log[2, NijckPC / NijcPC]]
- 73.7823
```

■

fCLL right summand

```
N[-beta * lambda * NijckPC
  (Log[2, NijckPC / (NijcckPC + NijckPC)] - Log[2, NijcPC / (NijcPC + NijccPC)])]
62.7106
```